Radiation from relativistic jets in blazars and the efficient dissipation of their bulk energy via photon breeding

Boris E. Stern\textsuperscript{1,2,3} and Juri Poutanen\textsuperscript{3}\textsuperscript{*}

\textsuperscript{1}Institute for Nuclear Research, Russian Academy of Sciences, Prospect 60-letiya Oktyabrya 7a, Moscow 117312, Russia
\textsuperscript{2}Astro Space Centre, Lebedev Physical Institute, Profsoyuznaya 84/32, Moscow 117997, Russia
\textsuperscript{3}Astronomy Division, Department of Physical Sciences, PO Box 3000, FIN-90014 University of Oulu, Finland

Accepted 2007 November 7. Received 2007 October 29; in original form 2007 September 19

ABSTRACT

High-energy photons propagating in the magnetized medium with large velocity gradients can mediate energy and momentum exchange. Conversion of these photons into electron–positron pairs in the field of soft photons with the consequent isotropization and emission of new high-energy photons by Compton scattering can lead to the runaway cascade of the high-energy photons and electron–positron pairs fed by the bulk energy of the flow. This is the essence of the photon breeding mechanism.

We study the problem of high-energy emission of relativistic jets in blazars via photon breeding mechanism using 2D ballistic model for the jet with the detailed treatment of particle propagation and interactions. Our numerical simulations from first principles demonstrate that a jet propagating in the soft radiation field of broad emission-line region can convert a significant fraction (up to 80 per cent) of its total power into radiation.

We show that the gamma-ray background of similar energy density as observed at Earth is sufficient to trigger the photon breeding. The considered mechanism produces a population of high-energy leptons and, therefore, alleviates the need for Fermi-type particle acceleration models in relativistic flows. The mechanism reproduces basic spectral features observed in blazars including the blazar sequence (shift of spectral peaks towards lower energies with increasing luminosity). The significant deceleration of the jet at subparsec scales and the transversal gradient of the Lorentz factor (so-called structured jet) predicted by the model reconcile the discrepancy between the high Doppler factors determined by the fits to the spectra of TeV blazars and the low apparent velocities observed at very long baseline interferometry (VLBI) scales. The mechanism produces significantly broader angular distribution of radiation than that predicted by a simple model assuming the isotropic emission in the jet frame. This helps to reconcile the observed statistics and luminosity ratio of Fanaroff–Riley type I (FR I) and BL Lac objects with the large Lorentz factors of the jets as well as to explain the high level of the TeV emission in the radio galaxy M87.

We also discuss other possible sites of operation of the photon breeding mechanism and demonstrate that the accretion disc radiation at the scale of about 100 Schwarzschild radii and the infrared radiation from the dust at a parsec scale can serve as targets for photon breeding.

Key words: acceleration of particles – radiation mechanisms: non-thermal – galaxies: active – BL Lacertae objects: general – galaxies: jets – gamma-rays: theory.

1 INTRODUCTION

The large gamma-ray isotropic luminosities of the blazars $10^{47}$–$10^{49}$ erg s$^{-1}$ (Mukherjee et al. 1997) require a very powerful energy source. There is a general consensus that this emission is produced...
by relativistic jets emanating from the vicinity of a black hole. The beaming of radiation into a solid angle \( \Omega \sim 0.01 \) sr reduces the total luminosity to \( 10^{45}-10^{46} \text{ erg s}^{-1} \), which is still comparable to the bolometric luminosity of a luminous quasar. This implies a high efficiency of the bulk energy conversion into gamma-ray emission, because the accretion luminosity is similar to the jet power (Rawlings & Saunders 1991).

What kind of energy is available for the high-energy radiation of blazars: the jet internal energy or the total energy carried by the jet through the external environment? The first scenario can be associated with the internal shocks (e.g. Rees 1978; Spada et al. 2001) or magnetic reconnection (see e.g. Lyutikov 2003). Then the efficiency is limited by the dispersion of the jet Lorentz factor or by the share of magnetic field which can reconnect, which depends on the field structure.

The second scenario provides a larger potential energy budget, but requires a ‘friction’ between the jet and the external environment. A promising mechanism for such a friction can be associated with the exchange of neutral particles between the two media which move with respect to each other. The simplest version of such scenario is the exchange of photons by Compton scattering (Arav & Begelman 1992). If the energy flux in the quasar jet is dominated by cold protons then the Thomson optical depth across the jet (assuming one electron per proton) is

\[
\tau_T(R) = \frac{L_j}{R^2 \sigma_T c^2 \Gamma_j^3} \approx 2.3 \times 10^{-5} \frac{L_{j,45}}{R_j / \theta_j},
\]

where \( L_j \) is the jet power, \( R_j \) is the radius of the jet cross-section, \( R \) is the distance from the black hole, \( \theta = R_j / R \) and \( \Gamma_j \) are the jet opening angle and the initial Lorentz factor.\(^1\) Such a small optical depth is insufficient to provide a considerable photon viscosity. However, the optical depth for high-energy photons against pair production on the low-energy photons can be high enough. For example, a luminous accretion disc of a quasar emitting soft radiation with luminosity \( L_d \sim 10^{45} \text{ erg s}^{-1} \) at a typical temperature \( \Theta = kT/m_e c^2 = 10^{-5} \), provides a high opacity across the jet (see Stern & Poutanen 2006, hereafter SP06):

\[
\tau_{\gamma\gamma}(R) = 60 \frac{L_{d,45}}{R_j \Gamma_j^3 \Theta_j} (10^6),
\]

which remains more than unity up to the parsec scale.

Derishev et al. (2003) and Stern (2003) suggested a mechanism of dissipation of the bulk energy of relativistic fluids through the particle exchange with charge conversion (the converter mechanism). When this mechanism supplies energy to \( e^\pm \) pairs and photons, it can work in a runaway manner similar to a chain reaction in a supercritical nuclear pile. Here the role of breeding neutrons belongs to the high-energy photons, which extract energy from the fluid and breed exponentially. In this way the converter mechanism takes the form of a supercritical photon breeding (hereafter, photon breeding). Stern (2003) studied numerically the operation of the photon breeding mechanism in ultrarelativistic shocks propagating in a moderately dense environment, showing the high efficiency of the bulk energy dissipation. A similar problem for relativistic jets in active galactic nuclei (AGN) was investigated by us (SP06), using a simple 1D ballistic model of the jet and a detailed treatment of particle propagation and interactions. We showed that up to 20 per cent of the jet kinetic energy can be converted into gamma-rays, if the following conditions are met: Lorentz factor above \( \sim 4 \), a sharp transition layer between the jet and the external environment, the presence of the ambient soft photon field, and a transversal or a chaotic, not very strong, magnetic field.

The present paper is a development of the approach presented in SP06. The main improvement is 2D treatment of the fluid (instead of 1D in SP06) and a better numerical resolution. The 2D treatment allows us to track the evolution of the system for much longer time, when it reaches a steady state. We also study the jet emission at a wider range of distances and with different sources of the soft photon background. We still neglect the internal pressure and treat the jet dynamics in a ballistic approximation.

In Section 2 we describe our model of the jet, the external soft radiation and the scheme of the numerical simulation. In Section 3 we describe the parameters of our simulations and present the results: the light curves of escaping photons, their spectra, distributions of the Lorentz factor of the decelerating jet and the energy distribution of pairs produced in the jet. The properties of the model and its limitations are discussed in Section 4. In Section 5 we discuss the astrophysical implications of our model. We conclude in Section 6.

2 PROBLEM SET-UP

2.1 Photon breeding mechanism

Let us first summarize the basic physics of the photon breeding mechanism in the context of relativistic jets (see SP06 for more details). Consider a jet with bulk Lorentz factor \( \Gamma_j \) propagating through the stationary medium. Assume that the medium is filled with the background soft photons [e.g. from the accretion disc, broad emission-line region (BLR), dusty torus, etc.] and some seed high-energy photons (e.g. extragalactic gamma-ray background). An external high-energy photon of energy \( \epsilon \) enters the jet and interacts with a soft (disc) photon producing an electron–positron pair.\(^2\) The typical energy of the high-energy photon interacting with the black-body radiation field of temperature \( \Theta \) is a few times \( \Theta^{-1} \). The time-averaged Lorentz factor of the produced pair (as measured in the external frame) gyrating in the magnetic field of the jet, becomes \( \gamma \sim \Gamma_j^2 \epsilon \sim \Gamma_j^2 \Theta^{-1} \). The electrons and positrons in the jet Comptonize soft photons (internal synchrotron or external) up to high energies.\(^3\) Some of these photons leave the jet and produce pairs in the external environment, which gyrate in the magnetic field and Comptonize soft photons more or less isotropically. Some of these Comptonized high-energy photons enter the jet again.

In this cycle, the energy gain, \( \sim \Gamma_j^2 \), is provided by the isotropization of the charged particles in the jet frame and is taken from the bulk energy of the flow. Other steps in the cycle are the energy sinks. The whole process proceeds in a runaway regime, with the total energy in photons and relativistic particles increasing exponentially, if the amplification coefficient (energy gain in one cycle) is larger than unity. As shown in SP06, the amplification coefficient is \( A \lesssim \Gamma_j^2 / 10 \), implying the minimum Lorentz factor of the flow needed for

\(^2\) The photon energies, in units of the electron rest mass \( m_e c^2 \), are denoted as \( x \) and \( \epsilon \) for photons of low (<1) and high (>1) energies, respectively. We define also the power-law index \( a \equiv -d \log F(x)/d \log x \), where \( F(x) \) is the photon energy flux.

\(^3\) Depending on the parameters the seed soft photons are either from the external medium or the synchrotron photons produced in the jet. In the first case, the inverse Compton (IC) scattered radiation is called the external radiation Compton (ERC) and in the second case, the synchrotron self-Compton (SSC).

---

\(^1\) We use standard notations \( Q = 10^q Q_0 \) in CGS units and for dimensionless variables.
therefore, difficult to reach as other conditions should be met.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

2.2 Model of the jet

We consider a jet propagating from the centre of the quasar accretion disc of luminosity $L_d$ through the medium filled with the soft photons from the disc as well as scattered in the environment. The total jet power scales with the disc luminosity $L_j = \eta L_d$. The comoving value of the magnetic field in the jet $B_j$ (its direction is transversal by assumption) is related to the Poynting flux carried by the (two-sided) jet

$$L_b = \eta B_j^2 \frac{8\pi}{c^2} 2\pi R_j^2 \Gamma_j^4 c \sim 8 \times 10^{33} B_j^2 R_j^2 (\theta \Gamma_j)^2 \text{erg s}^{-1},$$

(3)

which is assumed to be independent of distance (i.e. the magnetic field scales as $B_j \propto 1/R$). The ratio of the Poynting flux to the total jet power $\eta_B$ affects the ratio of synchrotron and Compton losses. The form of the rest of the energy content is not important in our approach as we ignore the internal pressure. We just assume that the jet does not contain high-energy interacting particles except those that are produced by the studied mechanism. If the rest of the jet energy is dominated by cold protons, the jet kinetic power (including the rest mass) is

$$L_k = (1 - \eta_B) L_j = \Gamma_j \dot{M} c^2 = 2\pi(R \theta)^3 \Gamma_j \dot{M} c^3 \eta_p,$$

(4)

where $\dot{M}$ is the mass outflow rate and $\eta_p$ is the proton concentration (in lab frame). The total jet power is then $L_j = L_b + L_k$.

2.3 External environment

2.3.1 Accretion disc radiation

As discussed in SP06, the photon breeder mechanism requires the existence of the external soft radiation field which is opaque for high-energy photons against pair production. The emission of the accretion disc is opaque for high-energy ($\sim 10^5$ MeV) photons moving across the jet up to the distance of a few parsec for the disc luminosity $L_d \sim 10^{45}$ erg s$^{-1}$. We characterize this radiation by the multicolour disc spectrum assuming a power-law $T(\sigma) = T_{\text{max}} (\sigma/\sigma_{\text{in}})^{-3/4}$ dependence of temperature on the disc radius $\sigma_j$, with the ratio of the outer to inner disc radius $\sigma_{\text{out}}/\sigma_{\text{in}} = 10^4$. Here $T_{\text{max}} = 5$ eV is the maximum disc temperature at $\sigma_{\text{in}} = 3R_b$ and $R_b = 2GM/c^2$ is the black hole Schwarzschild radius. The dimensionless maximal temperature is $\Theta_{\text{max}} = kT_{\text{max}}/m_e c^2 = 10^{-5}$. We neglect the expected dependence on the luminosity $T_{\text{max}} \propto L_{1/4}$ as it is a small effect.

At distances much larger than the disc size, the disc radiation is directed along the jet and does not interact with the gamma-rays produced in the jet. Thus the conversion of these gamma-rays into electron–positron pairs requires a source of transversal soft photons. Below we consider three possibilities for such sources at different distance scales.

2.3.2 External radiation

(i) Model A: This model represents the isotropic radiation from the BLR at a subparsec scale $R = 2 \times 10^{17}$ cm (as in SP06). The soft external radiation in this case is the disc radiation reprocessed and scattered by clouds in the BLR with an admixture of a softer infrared (IR) radiation from larger distances. The resulting spectrum has a complicated form, which we parametrize here (as in SP06) by a cut-off power law $F_{\text{BLR}}(x) \propto x^{-\alpha} \exp(-x/s_{\text{max}})$ extending from the far-IR $s_{\text{max}} \sim 10^{-8}$ to the UV band, as we assume $s_{\text{max}} = \Theta_{\text{max}}$.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.

The preferred conditions are: the weak jet magnetic field (which reduces the energy sink by synchrotron radiation) and large energy density of the external isotropic radiation in the jet frame (which increases the Compton losses). The latter requirement translates into high $\Gamma_j$ and/or high fraction of the disc radiation scattered/reprocessed in the ambient medium. A sufficiently sharp boundary between the jet and the external environmental also increases the efficiency of the process; however, as we show in this paper, it is not a necessary condition.
higher than that in the interstellar medium, but still realistic for the subparsec region of an AGN.

### 2.4 Model parameters

The efficiency of the considered mechanism depends not directly on the luminosities, but on the dimensionless compactness parameters. The compactness of the radiation and of the magnetic field can be defined as

\[ \ell = \frac{\sigma_T}{m_c c^2} U R_j, \]

where \( U \) is the corresponding energy density. The compactness is useful when estimating the cooling rate of pairs. The comoving magnetic compactness is defined as

\[ \ell_B = \frac{\sigma_e}{m_c c^2} \frac{B_j^2}{8\pi} R_j = 3.2 \times 10^{-3} B_j^2 R_{j,16} \]

\[ = 4.3 \times 10^{-3} L_{B,45} R_{j,16}^{-1} \left( \frac{\Gamma_j}{10} \right)^2. \]

The photon compactness, defined in the external frame, has two components: the direct accretion disc radiation

\[ \ell_d = \frac{\sigma_e}{m_c c^2} \frac{2L_d}{4\pi R_c^2} R_j = 4.3 \times 10^{-3} L_{d,45} R_{j,16}^2 R_{j,16} \]

with factor 2 in front of \( L_d \) coming from the Lambert law and the isotropic component \( \ell_{iso} = \eta_1 \ell_d \). With these definitions, we can write the equation for electron energy losses in the jet frame (for model A) as

\[ \frac{d\gamma}{dt} \approx -(\ell_B + \ell_{iso} \Gamma_j^2 + \ell_d / \Gamma_j^2) \gamma^2, \]

where the term with \( \ell_d \) describes the synchrotron losses and the second and third terms – the Compton losses (in Thomson limit) on the isotropic radiation field (with a factor \( \sim \Gamma_j^2 \) coming from the Lorentz transformation to the jet frame) and on the direct disc radiation, respectively. Because the soft photons can interact with high-energy pairs in Klein–Nishina regime, the second term in reality is much reduced. Equation (9) does not include SSC losses, which are zero at the beginning of the photon breeding cascade (because it takes time to build up the synchrotron energy density), but, in principle, can be significant in the steady-state regime. The pairs produced outside of the jet lose their energy mostly by Compton scattering of the disc radiation (the synchrotron losses are negligible because of the low magnetic field there) with \( \ell_d \) determining the cooling rate:

\[ \frac{d\gamma}{dt} \approx -\ell_d \gamma^2. \]

The jet compactness

\[ \ell_j = \frac{\sigma_T}{m_c c^2} \frac{L_j}{2\pi R_c} = 0.43 L_{j,45} R_{j,16}^{-1} \]

is related to the Thomson optical depth through the jet

\[ \tau_p = \frac{m_e}{m_p} \ell_j (1 - \eta_B) = 2.3 \times 10^{-3} (1 - \eta_B) L_{j,45} R_{j,16}^{-1} \Gamma_j^{-1} \]

\[ \left( \frac{\Gamma_j}{10} \right)^2. \]

### 2.5 Simulation method

#### 2.5.1 Radiative processes

The numerical simulation of radiative processes is based on the large particle Monte Carlo code described in Stern (1985) and Stern et al. (1995). The present version of the code handles Compton scattering, synchrotron radiation, photon–photon pair production, and pair annihilation. All these processes are reproduced without any simplifications at the microphysics level. Synchrotron self-absorption was neglected as it consumes too much computing power and is not important at the considered conditions. The number of large particles (LPs) is \( 2^{10} = 524,288 \) for most of the simulations (in SP06 we used \( 2^{17} \) LPs), which is still insufficient to completely get rid of numerical fluctuations. A substantially better resolution will require massive parallel computations and a smoothing technique which has to be developed.

#### 2.5.2 Particle kinematics

The scheme of particle tracking in the relativistic fluid was developed in Stern (2003) and described in details in SP06. The 4-momentum of electron/positron LPs are defined in the comoving frame of the fluid. If the electron/positron has a critical Lorentz factor

\[ \gamma_{max} \approx 10^8 B_j^{-1/2}. \]

it loses half of its energy in a half of Larmor orbit to synchrotron radiation. This requires a fine particle tracking at the first Larmor orbit for the comoving Lorentz factor of the particle \( \gamma > \gamma_{max} \), and, therefore, the comoving tracking step is limited to \( \Delta t = 0.1 R_j / c \), where \( R_j = 1.7 \times 10^3 \gamma / B_j \) cm is the Larmor radius.

In the external medium, synchrotron losses are small and an electron is cooled by the disc radiation. The condition that the electron cooling time-scale is longer than the inverse of Larmor frequency can be written as

\[ \frac{1}{\gamma \ell_d} > \frac{2\pi R_j}{R_j}, \]

which translates to the limit on the Lorentz factor

\[ \gamma < \gamma_{ext.max} = 10^6 \left( \frac{R_{j,16} R_{ext,-3}}{\ell_{d,-3}} \right)^{1/2}. \]

In our simulations, we exactly track the particle motion for the duration of the first Larmor orbit for the comoving \( \gamma > 2 \times 10^7 \). For smaller \( \gamma \) and at further orbits we neglect the dependence between the comoving direction and the energy and sample the direction of the particle assuming a uniform distribution of its gyration phase in the comoving system (see details in SP06).

The trajectories of electrons and positrons in the magnetic field are simulated assuming a random direction of the field in the plane normal to the direction of motion of the jet as well as in the external matter. The magnetic field correlation length is assumed to be larger than the Larmor radius.

#### 2.5.3 Geometry and jet dynamics

Our model of the jet is the same as in SP06 except now we use 2D representation of the fluid instead of the 1D. We consider a piece of the jet centred at distance \( R \) from the central source and length \( 20 R_j \), where the jet radius is \( R_j = \theta R \) and \( \theta \) has the meaning of the opening angle, while for simplicity we approximate the jet by a cylinder of radius \( R_j \). The boundary condition at the inlet is the flow of constant Lorentz factor \( \Gamma_j \) (see Fig. 1).\(^4\)

\(^4\)Our model assumes a well-collimated jet with \( \theta \lesssim 1/\Gamma_j \). If the opening angle of the jet is much larger, then the efficiency of photon breeding drops, because the probability for the high-energy photons to escape the jet decreases.
1. The simulation volume of radius \( s \) is measured in units of \( L = 10 \) at \( z = 0 \), and small Poynting flux.

We introduce dimensionless coordinates, where the transversal distance from the jet axis \( r \) and the distance from the central source \( z \) are measured in units of \( R \). We use a fixed Euler grid with fairly rough spacing: 20 cells in the \( z \) direction and 64 cells in the \( r \) direction. The step on \( r \) is non-uniform: the spacing is finer near the jet boundary. The time unit is \( R/c \).

The fluid in each cell \( i \) is characterized by its total energy \( E_i \) and momentum \( P_i \), which define the cell Lorentz factor:

\[
\Gamma_i = \frac{E_i}{\sqrt{E_i^2 - P_i^2}}.
\]

The flow is treated as 1D along the cylinder axis, because the transversal component of \( P_i \) never exceeds \( 10^{-2} \) of the total momentum and the transversal displacement of the flow can be neglected.

2.5.4 Statistical representation

For a good statistical representation of the process, it is necessary to have more or less constant density of the LPs over the volume of the cylinder. As the energy (and number) density of particles (pairs and photons) grows by orders of magnitude from the inlet of the cylinder to the outlet, we need to introduce the dependence of statistical weights on \( z \). The statistical weight \( w \) of a particle of energy \( \epsilon \) is defined through the energy content \( w = 2^s \), where \( n \) is the integer part of \( z/2 \) for \( z < 14 \) and \( n = 7 \) at \( z > 14 \). The value \( s \) varies with time in order to keep the total number of LPs approximately constant. This weighting scheme is implemented as follows: we split a particle into two identical particles with twice less statistical weight when it crosses one of the planes \( z = 2, 4, 6, \ldots \) in the direction opposite to the jet motion and we kill a particle with probability 0.5 and increase its weight by 2, when it crosses the plane in the direction of jet motion. The price for a good resolution at the region, where the avalanche starts and grows, is a poor resolution at the output. For that reason the Poisson noise in output light curves and photon spectra is rather high.

2.5.5 Simulation set-up

At the start of simulations we set constant Lorentz factor \( \Gamma_j \) over the jet volume \( r < 1 \) and \( 0 < z < 20 \), see Fig. 1) and assume a sharp boundary between the jet and the surrounding medium. We also inject a number of high-energy photons with the total energy several orders of magnitude smaller than the steady-state luminosity of the jet. (There is no injection of any additional photons later during the simulations and the high-energy population of particles is self-supporting.) The external soft-photon radiation field is constant during the simulation.

Interactions between particles change the energy and momentum of the fluid. The electron–positron pairs born in the process become part of the fluid. The momentum and energy exchange between photons and each grid cell of the flow is accumulated during the time step \( \Delta t = 0.01R/c \) and the total 4-momentum of the cell is updated after that. The momentum is transferred between cells along the jet axis.

The output of the simulations consists of the photons that escape from the cylindrical ‘simulation volume’ with the boundaries \( r = 1.5 \) and \( z = 0 \) and 20. We also record the energy spectrum of photons and pairs in the simulation volume.

3 RESULTS

3.1 Simulation runs

We consider the distance scale of \( R = 10^{16}–10^{20} \) cm and the jet Lorentz factor \( \Gamma_j \approx 8–40 \). We vary the luminosity of the accretion disc \( L_d \) in the interval \( 10^{33}–10^{40} \) erg s\(^{-1}\) and try different ratios of the jet to the disc power. First, we present results of three series of simulations, where we vary one of the parameters and nine non-systematic runs covering a wider area of parameters to demonstrate the working area of the mechanism. In the two series we vary the disc and jet luminosity, while in the third series we vary the jet Lorentz factor. Most of our simulation runs concern model A. Three runs correspond to different astrophysical scenarios described by models B and C, where the photon breeding operates.

(i) Runs 01–05: This series represents magnetically dominated jet (i.e. \( \eta_B = 1 \)) with the jet power equal to the disc luminosity (\( \eta_j = 1 \)), which is varied between \( L_d = 3 \times 10^{45} \) erg s\(^{-1}\) down to \( 3 \times 10^{41} \) erg s\(^{-1}\), where the photon breeding becomes subcritical and the process does not work (at \( R = 2 \times 10^{17} \)).

(ii) Runs 10–16: Similar to the previous series, but for the matter dominated jet with \( \eta_B = 0.2 \) and \( \eta_j = 1 \). We vary \( L_d \) in a wider range, because the process for smaller \( \eta_B \) has a lower luminosity threshold.

(iii) Runs 21–25: In this series we have fixed the disc luminosity to \( L_d = 3 \times 10^{44} \) erg s\(^{-1}\) use \( \eta_j = 1 \) and \( \eta_B = 0.2 \), and vary the initial Lorentz factor of the jet.

(iv) Runs 30–35: Run 30 demonstrates a photon breeding process starting from the extragalactic gamma-ray background and resulting in 20 orders of magnitude growth of the high-energy photon population (see Section 4.5). Run 31 represents a strongly non-linear system, where the jet power exceeds the disc luminosity. Run 32 is the case of the weakest AGN (\( L_d = 2 \times 10^{39} \) erg s\(^{-1}\) ) tried in this work for model A. Run 33 demonstrates that a high efficiency can be achieved at \( \Gamma_j = 10 \) if the magnetic field is weak. Run 34 is a trial with the lowest Lorentz factor, \( \Gamma_j = 8 \), and small Poynting flux. Run 35 is similar to run 12, but for the harder spectrum of isotropic external photons (\( \alpha = 0 \) instead of \( \alpha = 0.4 \)).

(v) Runs 41–42: They correspond to model B, where we simulate interaction of a strong jet \( L_j = 2.3 \times 10^{45} \) erg s\(^{-1}\) of Lorentz factor \( \Gamma_j = 20 \) with the IR radiation (\( \Theta = 10^{-7} \)) of the dusty torus at a parsec scale. Run 43 describes Model C, where a relatively weak, \( \eta_j = 0.1 \), jet interacts with the direct radiation from the accretion disc of \( L_d = 8 \times 10^{44} \) erg s\(^{-1}\) at a distance of a hundred gravitational radii (for a 10\(^{8}\) solar mass black hole).

The parameters for these runs are summarized in Table 1.
### Time evolution and the steady-state regime

The energy release curves for set 2 (runs 10–15) are presented in Fig. 2. All curves show an exponential rise at the start with the time constant depending on the disc luminosity. The fast exponential rise turns to a slower growth when approaching the steady state. A very fast rise (time constant $\sim 0.1 R_*/c$ for run 10) occurs in the case of a dense external radiation field when the photon free path length is much smaller than the jet radius. Then the photon breeding takes place only in a narrow layer at the jet boundary. Such fast breeding terminates after a short time, when the thin boundary layer decelerates. The breeding turns to a slower mode, where the softer photons with a longer free path dominate.

Note that the injection of external high-energy photons takes place only at the start of the simulation. Then the regime becomes self-supporting. The reason for this is a spatial feedback loop. The photon avalanche develops from a smaller to a large $z$, but some high-energy photons produced in the external environment move in the opposite direction, from larger $z$, where there are many high-energy photons, to smaller $z$, where they can initiate a new photon avalanche. Due to this feedback a high efficiency of emission $\varepsilon_{\text{eff}} = L_{\text{ph}}/L_\gamma$ can be reached even if the growth of the photon avalanche is slow.

![Figure 2](image_url)
if the magnetic field is very weak. Below this threshold the photon–photon opacity across the jet (see equation 2) becomes insufficient. (We note here that the working luminosity limits are given for $R = 2 \times 10^{17}$ cm, $\Upsilon_j = 20$ and $\eta_i = 0.05$.)

Remarkably, the efficiency at a moderate disc luminosity ($\sim 3 \times 10^{44}$ erg s$^{-1}$; run 13) is higher than for a more luminous quasar (runs 10, 11 and 31). The reason is that at a high luminosity the spine of the jet is shielded from the high-energy external photons by the opaque (respectively to pair production) radiation of the accretion disc and synchrotron radiation of pairs in the jet. In runs 10 and 31, only the photons with energy $\epsilon < 10^3$ can penetrate deeply into the jet. Nevertheless, such moderate energy photons still can interact with the synchrotron photons (mostly produced in the decelerated outer jet layers) inside the jet and support the photon breeding.

As one can expect, the dependence on $\Upsilon_j$ is very strong. The efficiency $\varepsilon_{\text{eff}}$ is close to $\Upsilon_j = 1/\Upsilon_j$, where the average Lorentz factor at the outlet $\Upsilon_j$ slightly decreases when $\Upsilon_j$ increases (see Section 3.4).

At a lower $\Upsilon_j$ the process becomes very sensitive to the ratio of the Poynting flux to the isotropic disc luminosity. Indeed, at the given magnetic flux $L_0$, the comoving magnetic compactness scales as $\epsilon_{\text{eff}} \propto L_0^{1/2}/\Upsilon_j^2$ (see equation 7), while Compton cooling rate in the Thomson limit scales as $\propto \epsilon_{\text{eff}} \Upsilon_j^{1/2}$, see equation (9). Thus the ratio of Compton to synchrotron losses scales as $\eta_j \Upsilon_j^{3/2}/\epsilon_{\text{eff}}$. This ratio decreases somewhat because of the Klein–Nishina effect, but it is still a strong function on $\Upsilon_j$. That is the reason why the runaway photon breeding does not happen at $\Upsilon_j < 14$ if $\eta_i = 0.2$ (series 21–25). If the magnetic field is very weak, then the process can work efficiently at $\Upsilon_j = 10$ (run 33) and less efficiently, but still in a self-supporting regime at $\Upsilon_j = 8$ (run 34).

All results described above are obtained under an assumption that the BLR is relatively abundant with isotropic IR photons, so that the photon spectrum can be roughly approximated as a cut-off power law with $\alpha = 0.4$ (see Section 2.3.2). The spectrum however can be harder if, for example, there is no sufficient amount of dust around the AGN. Therefore, we made a couple of trials for model A with a harder BLR spectrum, $\alpha = 0$. One trials with the same parameters as run 13 ($L_0 = L_j = 3 \times 10^{44}$ erg s$^{-1}$) resulted in no self-supporting photon breeding. Another trial with ($L_0 = L_j = 10^{43}$ erg s$^{-1}$ (run 35 in Table 1) demonstrated photon breeding, which was slower than in run 12 (with $\alpha = 0.4$). However, the final steady state was almost the same including the radiative efficiency (0.41 versus 0.5 in run 12) and the emitted spectrum. Such a striking difference between the two cases differing only by a factor of 3 in luminosity appears because of the non-linear character of the mechanism for high-power jets: soft synchrotron photons produced by the jet significantly contribute to the photon–photon opacity. The problem with soft photon starvation can be resolved if some internal jet activity (e.g. internal shocks) supply soft synchrotron photons which can be then scattered in the BLR (Ghisellini & Madau 1996).

In general, the results of our simulations for distance $R$ from the black hole and luminosity $L_j$ can be scaled to another distance $R'$ if one changes at the same time all luminosities as $L' = LR'/R$. In this case, the compactness of all radiation components and of the magnetic energy does not change (see equation 6). Such scaling is not exact, because the value of magnetic field changes and the synchrotron spectra change accordingly. The scaling, however, does not affect the criticality of the system as long as the ratio between synchrotron and Compton losses remains constant. At luminosity smaller than about $L_{d,\text{min}} \approx 10^{44}R_j^{3/2}$ erg s$^{-1}$ the opacity for pair production through the jet becomes smaller than unity and the supercriticality condition breaks down. Assuming the

---

**Figure 3.** The escaping photon luminosity in units of the jet power versus time for runs 10, 11, 21 and 31. Note that the light curves look different compared to Fig. 2 as it takes about 20 time units for photons to escape from the simulation cylinder (and the ordinate scale is linear here).

We can see large fluctuations of the energy release at the saturation regime (at the stage of the exponential rise, the curves are smooth). Fluctuations have the Poisson component which is large because of the weighting method: LPs at the outlet have statistical weight $2^L$ larger than at the inlet. There are also non-Poisson fluctuations which are caused by fluctuations in the spatial feedback: a photon with a large statistical weight moves from the end of the active jet fragment to its beginning, interacts there and produces a photon avalanche. The number of such photons is small, but the amplification coefficient (i.e. the number of secondary photons and pairs) can exceed $10^4$. Therefore the number of LPs as large as $\sim 10^6$ is still insufficient for a good statistical representation.

However, statistical noise is not the only reason for the large fluctuations in the output photon flux. In runs 10 and 31, where the compactness is high, and especially in run 31, where the system is strongly non-linear, we see a large amplitude variability at a range of time-scales (see Fig. 3). We performed run 31 with the different number of LPs: $2^{19}$ and $2^{21}$, but the character and the amplitude of the fluctuations was similar. Thus, in this case we deal with the real instability of a non-linear dynamical system (see Section 4.2 for discussion).

### 3.3 Radiative efficiency and the ‘working area’ of the process

The resulting efficiency of the conversion of jet power into radiation in the steady state and the time constant of the exponential photon breeding are shown in the last columns of Table 1. Once we fixed $R, R_j$ and the ratio $\eta_i$ in all runs for model A, our main remaining parameters are the jet Lorentz factor, the disc luminosity and the Poynting flux. The jet power is not important unless it exceeds the disc luminosity (as in run 31), making the system strongly non-linear. The series of runs 01–05 shows that the process can work efficiently in the case of a magnetically dominated jet giving $\varepsilon_{\text{eff}} \approx 1/4$. The lowest luminosity when it works is $\sim 10^{44}$ erg s$^{-1}$. If the matter dominates over the magnetic energy by a factor of 5 (runs 10–16) then the radiative efficiency is higher, above 50 per cent, and the working luminosity range slightly extends down to $5 \times 10^{43}$ erg s$^{-1}$. The supercritical breeding is still possible at even lower disc luminosity, $2 \times 10^{43}$ erg s$^{-1}$ (see run 32), but only...
distance to the emission region of $R \sim 10^3 R_9$, we can express the luminosity threshold in terms of the Eddington luminosity $L_{\text{d, min}} \sim 10^{-5} L_{\text{Edd}}$.

The distance to the BLR may also depend on the luminosity of the object. The reverberation mapping gives the relation $R_{\text{BLR, 17}} \approx L_{\text{d, 44}}^{1/2}$ (Peterson 1993; Kaspi et al. 2005). This then gives the condition $L_{\text{d, 44}} > 0.1 L_{\text{Edd}}^{1/2}$, which translates to the lower limit on the luminosity $L_{\text{d}} > 10^{52} \text{ erg s}^{-1}$, when the photon breeding can operate.

The conditions when model A operates can be summarized as follows.

(i) At $\Gamma_j \gtrsim 20$ and at $L_{\text{d, 44}} \sim L_{\text{d, 44}} \gtrsim 5 R_{\text{17}}$, the photon breeding mechanism is efficient and very robust: it works independently on the share of magnetic energy in the jet and is not sensitive to the spectrum of the external radiation.

(ii) At $\Gamma_j \gtrsim 20$ and lower jet power $L_{\text{d, 44}} < 5 R_{\text{17}}$, when the disc luminosity is still sufficiently high, $L_{\text{d, 44}} > 0.5 R_{\text{17}}$, the mechanism is sensitive to the spectrum of isotropic radiation in the BLR and, if there is a deficit of soft photons, the photon breeding is not self-supporting.

(iii) For $\Gamma_j < 20$ the mechanism becomes sensitive to the magnetic field in the jet. The strong field inhibits the photon breeding. When the magnetic energy is much smaller that the matter kinetic energy, the efficient emission is possible down to $\Gamma_j \approx 8$.

(iv) The threshold of the disc luminosity is $L_{\text{d, 44}} \sim 0.1 R_{\text{17}}$. However, the self-supporting emission at such low $L_{\text{d}}$ requires weak magnetic field and a soft spectrum of the BLR radiation.

We have also tried models B and C just to show that the process can work in different situations. Radiative efficiencies of 20 per cent are easily reached. We do not perform a systematic study of these models because both scenarios depend on various conditions that require a different study. Model C, for example, should be considered together with the mechanism of the jet launching and in model B one should account for the history of the jet flow before it reaches the parsec-scale distance.

### 3.4 Jet deceleration and the energy release

Jet deceleration in the 1D approach of SP06 took place mainly near the jet boundary ($r > 0.9$), while the centre of the jet was not affected.

In the 2D simulations we can track the deceleration of the deeper parts of the jet up to its axis. The transversal distributions of the fluid Lorentz factor for runs 21–24 are shown in Fig. 4. Distributions of $\Gamma$ along the jet axis are shown in Fig. 5. It is remarkable that the terminal Lorentz factor $\Gamma_f$ depends weakly on the initial $\Gamma_j$, actually it even decreases when $\Gamma_j$ increases.

The highest gradient of the Lorentz factor is near the jet boundary. In run 22, the Lorentz factor near the boundary drops from 30 down to 5 at $z = 3$ (see Fig. 5). The jet experiences similar deceleration in runs 01, 10, 11 and 31, where the radiation density is high. At the outlet the gradient of $\Gamma_f$ depends weakly on the distance from the axis. It reaches some critical value beyond which the photon breeding is not effective anymore. In cases of a lower compactness (runs 04, 14, 15, 32) the Lorentz factor changes more smoothly with $z$. At the outlet, $d\Gamma_f/dr$ is still large close to the boundary, with the jet getting the form of a fast spine and a slow sheath. A large gradient of $\Gamma$ means that our ballistic approximation rapidly breaks down in

![Figure 4](image1.png)  
(a) The transversal distribution of the bulk Lorentz factor. (a) Dependence on distance $z$ for run 22 (curves from top to bottom correspond to $z = 2$ with step 2 till $z = 20$). (b) Distribution of the terminal Lorentz factor at the outlet ($z = 20$) for runs 21–24 corresponding to $\Gamma_j = 40–14$.

![Figure 5](image2.png)  
(b) Distribution of the fluid Lorentz factor in $z$ direction for runs 21–24. Solid curves show the Lorentz factor at the jet axis $r = 0$, and the dashed curves are for the jet boundary at $r = 0.99$. 

3.5 Radiation spectra

Fig. 6(a) shows the output spectra of photons emitted in the direction of the jet ($\theta < 10^\circ$). The spectra (except those for runs 10 and 31 with very high compactness) show a two-component synchrotron–Compton structure. Runs 01–03 produce a synchrotron peak in the range $\epsilon \sim 10^{-3} - 10^{-1}$, consistent with those observed in BL Lacs, however, the theoretical peaks are less prominent that the observed ones (detailed comparison with the observed spectra is presented in Section 5.1), partially due to averaging over angles. The Compton component at high $L_s$ and $L_f$ (runs 01, 02, 10–12, 31) has a cut-off at $10^4 < \epsilon < 10^5$ due to the photon–photon absorption: the external isotropic BLR radiation provides a larger than unity optical depth for the high-energy photons.

The spectra for a smaller compactness (runs 04, 14, 15, 32, as well as runs 41, 42, where the compactness is small because of large $R$), have prominent synchrotron peaks at high energies $\epsilon \sim 10^{2} - 10^{3}$. The synchrotron and Compton components are clearly separated above the maximal energy of synchrotron radiation:

$$\epsilon_{s,\text{max}} \sim \gamma j_{\text{max}}^2 B_j / B_s \approx 230 \gamma,$$

(17)

which does not depend on the magnetic field (here $B_j = 4.4 \times 10^{13}$ G is the critical field). The value of $\gamma_{\text{max}}$ given by equation (13) is defined as the maximal electron energy (in the jet frame) after half the Larmor orbit, i.e. when it turns around from the counterjet direction to the jet propagation direction (see SP06). The derived $\epsilon_{s,\text{max}}$ assumes that the magnetic field is uniform at the scale of the electron Larmor radius and is transversal to the jet. It is not sensitive to the soft radiation field because an electron with the comoving Lorentz factor $\gamma \gtrsim 10^3$ interacts with the external radiation in the deep Klein–Nishina regime and the synchrotron losses dominate. Thus, the model predicts a new spectral feature which, in principle, can be observed by GLAST. Its detection would be a clear signature of the photon breeding mechanism (a distribution of diffusively accelerated electrons will hardly extend to the energy, where the electron loses a large fraction of its energy in one Larmor orbit). Moreover, because of independence of $\epsilon_{s,\text{max}}$ of the magnetic field and other parameters, the Lorentz factor of the jet can, in principle, be determined from the detailed fits of the shape of the spectral cut-off.

For the considered model parameters, the dominant source of seed soft photon for Compton scattering is BLR. At the start of simulations, the SSC losses are small, because the synchrotron energy density needs to be built up from zero. In the steady-state regime, the ratio of the SSC to the synchrotron losses can be expressed as $\epsilon_{\text{tot}}$ $\eta_{s,\text{KN}} / \eta_{s,\text{BLR}}$, where $\eta_{s,\text{KN}}$ is the fraction of soft synchrotron radiation (i.e. Comptonized in Thomson regime) in the total jet luminosity. We can estimate from Fig. 6(a) that $\eta_{s,\text{KN}}$ < 0.3 for runs 01–03 (with $\eta_{s,\text{BLR}} = 1$) and $\eta_{s,\text{KN}}$ < 0.1 for runs 10–12 (with $\eta_{s,\text{BLR}} = 0.2$). For a lower jet and disc luminosity (runs 03–04, 13–15), the electrons in the jet have higher energies and the SSC losses are suppressed by the Klein–Nishina effect. Therefore the SSC losses are always at least a few times smaller than the synchrotron losses and usually are much smaller than the ERC losses. However, the Compton losses of pairs in the fast spine of the jet on the synchrotron photons from the slower sheath can be considerable, at least in runs 10 and 31 with the highest compactness. These cases can be considered as intermediate between SSC and ERC.

The radiation spectra at large angles relative to the jet axis are shown in Fig. 6(b). We again see two-component, synchrotron and Compton spectra. The total (angle-integrated) luminosity in the gamma-rays emitted at large angles to the jet axis is about two orders of magnitude smaller than that of the beamed emission, which approximately corresponds to the gain factor $\Gamma^2$. The radiation spectra emitted as a function of the angle $\theta$ between the line of sight and the jet axis are shown in Fig. 7. We see that the synchrotron peaks shift to lower energies at larger angles and the two components are better separated.

3.6 Angular distributions of radiation

3.6.1 Radiation from isotropic pairs in the steady jet

Let us first discuss what kind of angular distributions can be expected from a steady (narrow) axisymmetric jet in relativistic motion. The observed bolometric luminosity is related to the emitted one (in the

Figure 6. Spectra of the escaping photons (angle-integrated) for runs 01–04 (upper panel) and runs 11–15 (lower panel). (a) Radiation spectra emitted along the jet axis with $\theta < 10^\circ$. (b) Radiation spectra at large angles to the jet axis, $\theta > 40^\circ$. © 2007 The Authors. Journal compilation © 2007 RAS, MNRAS 383, 1695–1712
jet frame) by the relation (see e.g. Lind & Blandford 1985; Sikora et al. 1997)

\[ L(\theta) \equiv \frac{dL}{d\Omega} = \frac{\delta^3}{\Gamma_j} \frac{dL'}{d\Omega'}. \]  

where \( \delta = 1/\Gamma_j(1 - \beta_j \cos \theta) \) is the Doppler factor, and \( d\Omega = d\phi d\cos \theta \). Let us define the amplification factor as the ratio of the observed and emitted luminosities

\[ A(\theta) \equiv \frac{L(\theta)}{L'/4\pi}. \]  

If the radiation source is isotropic in the jet frame, then \( dL'/d\Omega' = L'/4\pi \), and

\[ A(\theta) = \frac{\delta^3}{\Gamma_j}. \]  

Integrating over angles, we can verify that the total emitted and observed powers are the same. Equation (20) can be applied, for example, to the synchrotron radiation in a tangled magnetic field or to the SSC radiation by isotropic electrons.

If soft photons are isotropic in the external medium, they are strongly beamed in the direction opposite to jet propagation in the jet frame. This results in the angular distribution of the radiation IC scattered by relativistic isotropic electrons (see e.g. Rybicki & Lightman 1979)

\[ \frac{dL'}{d\Omega'} = \frac{L'}{4\pi} \frac{3}{4} (1 + \cos \theta')^2, \]  

with \( \theta' \) being the angle to the direction of jet propagation. For small \( \theta \), we can rewrite \( 1 + \cos \theta' \approx \delta/\Gamma_j \), and we get a much sharper angular dependence of the ERC radiation (see also Dermer 1995, and Fig. 8):

\[ A(\theta) = \frac{3}{4} \frac{\delta^5}{\Gamma_j^3}. \]  

Now the integration over all solid angles shows that the total observed power is \( 3/2 \) larger than the emitted one, which results from the non-zero net momentum of the emitted radiation in the jet co-moving frame (21).

\[ \text{Figure 7.} \] Intensity of radiation (per unit solid angle) at different angles to the jet axis for run 01.

\[ \text{Figure 8.} \] Luminosity (per unit solid angle) as a function of angle between the light of sight and the jet axis for run 01 in the three energy bands: IR–optical \( (\epsilon < 10^{-5}) \), X-rays \( (10^{-5} < \epsilon < 10^{-1}) \) and GeV gamma-rays \( (\epsilon > 10^3) \) (histograms, arbitrary normalization). The theoretical dependencies (20) expected for the steady relativistic jet emitting isotropically in the comoving frame shown by solid (black) curves (cases with \( \Gamma = 2 \) and 20). Dashed curves represent the synchrotron and SSC emission from pairs in 2D circular motion, given by equation (24). The solid (red) curve describes the jet ERC radiation from isotropic pairs (equation 22), while the dotted (red) curve is for the jet ERC radiation from 2D pairs (equation 26). The dot-dashed curve represents the emission of isotropic pairs in the external medium Comptonizing radiation beamed along the jet (equation 29). The emission from 2D pairs in the external medium is shown by long dashes (IC of beamed emission, see equation 28) and short–long dashes (synchrotron as well as IC of the isotropic photons, see equation 27).

3.6.2 Radiation of primary pairs

In the above we assumed explicitly an isotropic electron distribution. However, if the jet magnetic field has a transversal geometry (as assumed in this paper), the distribution may significantly deviate from the isotropic one. For example, the first generation of pairs, produced in the jet by the external high-energy photons (which are beamed in the jet frame similarly to the external soft photons), has a very narrow distribution of pitch angles around \( \pi/2 \). Let us now derive the angular distribution of radiation expected from these ‘2D’ pairs.

The pairs gyrating in a transversal magnetic field have a flat distribution in \( \theta \) (not \( \cos \theta \)). Therefore, their synchrotron emission has a pattern

\[ \frac{dL'}{d\cos \theta'} = L' \frac{1}{4\pi} \frac{1}{\pi \Gamma_j \sin \theta'}. \]  

An identical distribution would be produced by SSC emission (because the synchrotron photons that are Comptonized by 2D pairs are mostly produced by the next generation, lower energy, isotropic pairs). With the relation \( \sin \theta' = \delta \sin \theta \), we get the amplification factor (see dashed curves in Fig. 8)

\[ A(\theta) = \frac{1}{\pi \Gamma_j} \frac{\delta^2}{\sin \theta}. \]  

This distribution has sharp peaks at \( \theta = 0 \) and \( \pi \).

The external radiation IC scattered on 2D pairs produces a pattern

\[ \frac{dL'}{d\cos \theta'} = \frac{L'}{4\pi} \frac{2}{3\pi} \frac{(1 + \cos \theta')^2}{\sin \theta'}. \]  

which gives the distribution of the observed emission with the peaks at $\theta = 0, \pi$ (see dotted curve in Fig. 8):

$$A(\theta) = \frac{2}{3\pi} \frac{\delta^4}{\Gamma_j} \frac{1}{\sin \theta}.$$  

(26)

3.6.3 Radiation from external environment

In addition to the radiation from the jet, there is also radiation from the relativistic pairs produced in the external environment. They also have two populations. The first population is produced by the high-energy photons from the jet propagating a small angles to the jet direction $\theta \lesssim 1/\Gamma_j$. They perform 2D circular motion in the transversal magnetic field of the surrounding. The second population produced by the pair cascade is nearly isotropic.

The synchrotron radiation of 2D pairs follows distribution (23), with $\theta'$ replaced by $\theta$ (see short–long dashes in Fig. 8):

$$L(\theta) \propto \frac{1}{\pi \sin \theta}.$$  

(27)

The IC scattered isotropic BLR photons have the same distribution.

However, because most of the seed photons (synchrotron photons from the jet or the accretion disc photons) are beamed in the direction of the jet, the IC emission by the external pairs follows the distribution (25) with $\theta'$ replaced by $\pi - \theta$ (see long dashes in Fig. 8):

$$L(\theta) \propto \frac{\delta^4}{\sin \theta}.$$  

(28)

Thus, the 2D pairs produce a sharp peak at $\theta = \pi$.

The emission of isotropic pairs Comptonizing the disc (or jet synchrotron) radiation follows the law (21) with $\theta'$ replaced by $\pi - \theta$ (see dot–dashed curve in Fig. 8):

$$L(\theta) \propto \frac{3}{4} (1 - \cos \theta)^2.$$  

(29)

And, finally, isotropic pairs scattering isotropic radiation obviously produce a flat distribution of $L(\theta)$.

3.6.4 Emission pattern: simulations

As an example of the angular distribution of radiation predicted by the photon breeding model, we present results for run 01. The histograms in Fig. 8 show the dependence of the luminosity in three typical energy bands (IR–optical, X-ray and gamma-rays). We see that the distribution of high-energy photons at small $\theta$ follows quite closely that expected from the jet of $\Gamma_j = 20$ emitting isotropically in its rest frame (e.g. SSC, given by equation 20). The ERC radiation from the jet is more beamed (see equation 22 and the red solid curve in Fig. 8). An excess at $\theta = 0$ can be explained by the contribution of the SSC and ERC emission from 2D pairs (given by equations 24 and 26, respectively; see dashed and dotted curve in Fig. 8). At angles $\theta \gtrsim 0.45$, another component is obvious. This large-angle component is nearly isotropic and its flux at infinity is 4.5 orders of magnitude smaller than the average flux observed within the jet opening. For the run 01 with $\Gamma_j = 20$, the observed luminosity of this large-angle component at $\theta = \pi/2$ exceeds the luminosity given by expression (20) by more than three orders of magnitude. This off-axis emission is produced by the pairs gyrating in the external environment via Compton scattering of the disc and BLR photons and synchrotron photons from the jet. A peak at $\theta = \pi$ can be well described by IC emission of 2D pairs in the external environment (see long dashes and short–long dashes in Fig. 8) given by formulae (27) and (28).

The low-energy (IR–optical and the X-rays) photons are much less beamed. The spatial gradients of $\Gamma$ is the main cause of that. For example, the average $\Gamma$ of the inner half of the jet volume with $r < 0.7$ in run 01 is about 18, while the outer 20 per cent move with $\Gamma \lesssim 10$, dropping to $\Gamma \sim 2$ in the outer 5 per cent (see also Figs 4 and 5).

The soft band is dominated by the synchrotron radiation (Fig. 7). The emission at $\theta = 0.5$ exceeds the simple estimate (20) by three orders of magnitude. At angles $\theta \gtrsim 1/\Gamma$ = 0.05 the emission is mostly produced in the slower, decelerated layers of the jet (see Fig. 4), and the emission at $\theta \gtrsim 0.5$ is produced in the layers of $\Gamma \sim 2$. The synchrotron from 2D pairs in the jet even produces a peak at $\theta = \pi$. Some contribution to this peak is provided by the IC (low-energy tail) emission from the external medium.

The emission in the X-rays is the mixture of the synchrotron and ERC emission resulting in the intermediate behaviour seen in Fig. 8. The large-angle emission here is produced by IC in the external environment (see Fig. 7) and therefore has an angular dependence similar to that of the gamma-rays.

The sharp feature at $\theta = 0$ will be washed out if the jet is actually conical rather than cylindrical or the jet magnetic field is tangled. The tangled magnetic field in the external medium will also smooth out the predicted peak at $\theta = \pi$.

3.7 Pairs produced in the jet

The electron and positron comoving energy distributions averaged over time and jet volume for runs 01–04 and 10–15 are shown in Fig. 9. All spectra except that for run 15 have a clear low-energy cut-off at $\gamma_c = 10–10^2$, this is the energy the pairs cool down to in the dynamical time. The cut-off comoving energy assuming the Thomson regime for Compton cooling and neglecting SSC can be expressed as

$$\gamma_c = \frac{1}{t_{\text{dyn}} (\ell_0 + \ell_{\text{ec}} \Gamma^2)}.$$  

(30)

where $t_{\text{dyn}} \approx 10/\Gamma \sim 1$ is a typical (comoving) time the particles spend in the active cylinder. In our examples the Compton losses dominate over the synchrotron losses (see equation 9 and Table 1). For runs 04, 14 and 15 the cut-off is smoother because the cooling...
rate above $\gamma_s \sim 3 \times 10^3$ is affected by the Klein–Nishina regime, making it slower.

The spectrum above the cut-off is the standard cooling spectrum $\mathrm{d}N/\mathrm{d}y \propto \gamma^{-2}$, and it changes to a steeper slope at higher energies. This is the result of the pair cascade developing in the jet. The cascade pairs affect the energy distribution making it steeper $\mathrm{d}N/\mathrm{d}y \propto \gamma^{-3}$ (e.g. Svensson 1987) above the break energy $\gamma_b \sim 10^3$–$10^4$. Pairs of lower energies produce photons that can freely escape from the jet and the cascade steps. We may note here that most of the pairs in the jet are produced by photons emitted in the jet. Such process does not contribute to the energy release. However, during the cascade the typical photon energy decreases; it leads to the increase of the probability of the photon escape to the external environment. This in turn increases the efficiency of the jet energy dissipation.

Fig. 10 shows the fraction of the jet energy carried by generated pairs, which reaches 2–5 per cent. The number ratio of generated electrons and positrons to that of the protons increases with the jet power and for runs 14–10 it is $\tau_\pm/\tau_p = 0.017, 0.135, 0.63, 1.9, 4.0$, respectively.

4 PROPERTIES AND LIMITATIONS OF THE MODEL

4.1 Non-linear effects

There are two kinds of non-linearity in the problem: one appears because of the feedback of radiation on the fluid, another is the result of the synchrotron emission, which produces additional opacity for the high-energy photons. Here we consider the second one. The energy density of soft synchrotron radiation of pairs produced in the outer decelerated layers of the jet can exceed that of the external radiation. This in turn increases the efficiency of the jet energy dissipation.

In the case of substantial non-linearity, the process becomes self-supporting. The external radiation becomes unnecessary, because the stronger synchrotron radiation plays the same role. Stawarz & Kirk (2007) have studied this kind of non-linearity using kinetic equations and found that a source of high-energy photons quenches itself at high compactness. In our case, we see that the efficiency decreases at high compactness and the final spectrum gets softer. We can expect that such a tendency will continue with the increasing compactness.

The synchrotron emission from the jet scattered in the BLR (neglected in our simulations) can also affect the development of the cascade (Ghisellini & Madau 1996). The dominant contribution to the scattering is provided by the region of thickness $\sim R_j$ immediately adjacent to the jet. If we associate the fraction of radiation scattered/reprocessed in BLR, $\eta_s$, with the optical depth through the region of size $R$, then the optical depth through the layer of thickness $R_j$ for synchrotron photons moving at angle $1/\Gamma_j$ is of the order of $\tau_s \approx \eta_s \theta \Gamma_j$. We can write now the scattered luminosity as

$$L_s / L_j = \eta_s \tau_s = \eta_s (\eta_s L_j \eta_s \theta \Gamma_j),$$

where $\eta_s = L_s / L_j \lesssim 0.1$ is the fraction of the jet power emitted in the form of synchrotron radiation. Because the scattered synchrotron is escaping through the surface of $\sim 4\pi \theta R^2$, the ratio of its energy density to that of the BLR photons is

$$U_s / U_{BLR} \approx \eta_s \eta_s \Gamma_j.$$

This shows that the scattered synchrotron can be important for large $\eta_s$ or $\Gamma_j$. 

4.2 Temporal variability

In our simulations, we have assumed that the jet power and the Lorentz factor at the inlet do not change. However, because of the large non-linearity, the output photon flux demonstrates large non-Poisson fluctuations at different time-scales. At the present level of numerical resolution, it is difficult to distinguish confidently between numerical fluctuations and natural chaotic behaviour of the non-linear dynamical system. We just would like to emphasize that the latter possibility is very probable.

The transversal gradient of the Lorentz factor, \(d\Gamma/dr\), affects the rate of the photon breeding in the same way as the slope of a sand pile affects sand avalanches. The emitted radiation feeds back on the jet dynamics, making the gradient smoother. Thus \(d\Gamma/dr\) balances near its critical value in the same way as the slope of the sand pile does, when one pours sand on the top. It seems that we observe this in the cases of highest non-linearity, when the soft radiation of the jet dominates the external soft radiation (runs 10 and 31, see Fig. 11). It these cases the radiation power is more sensitive to the transversal gradient of \(\Gamma\) because of a short free path of high-energy photons in this direction.

If we assume a large fluctuation in the jet power at a time-scale shorter than \(R/c\Gamma^2\), the photon avalanche will be propagating along the jet and the observer will see a large increase in the luminosity partially because of the time compression. Simulations of strongly variable sources in the context of photon breeding model are left for future studies (see also SP06).

4.3 Impact on the external environment

The high-energy photons produced in the jet interacting outside of the jet deposit their momentum into the external environment and therefore accelerate it. This acceleration can be neglected if the density of the external matter is sufficiently high. Let the momentum deposited in a unit volume per unit time is \(\kappa(r, z) = dp/(dV dt)\). Then, equating the work of the photon pressure force to the kinetic energy of the flow one gets the final velocity of the entrained medium (in non-relativistic limit):

\[
\beta(r) = \frac{c}{v} = \left[\frac{2\int \kappa(r, z) dR}{nm_pc^2}\right]^{1/2},
\]

where \(n\) \(cm^{-3}\) is the particle density of the external medium. The required condition, \(\beta \ll 1\), allows us to put the lower limit of the density of the environment:

\[
n \gg n_{\text{cr}} = \frac{2\int \kappa(r, z) dR}{m_pc^2}.
\]

During the simulations we accumulate the average deposited momentum \(\kappa\). Its dependence on \(r\) is strong. For the layer closest to the jet, \(1 < r < 1.005\), we have \(\int \kappa(1 < r < 1.005, z) dR = 17\) erg \(cm^{-3}\) for run 31, which translates to \(n_{\text{cr}} = 2 \times 10^3\) \(cm^{-3}\). The requirement (34) seems reasonable for the BLR, where the cloud density is about \(10^9\) \(cm^{-3}\) (Osterbrock & Ferland 2006) and even the mean density should not be much smaller. The critical densities for other runs are even smaller: \(n_{\text{cr}} = 10^9\) \(cm^{-3}\) for runs 02 and 12, \(n_{\text{cr}} = 30\) \(cm^{-3}\) for runs 04 and 14. For runs 41 and 42, the required density is \(n_{\text{cr}} = 10\) \(cm^{-3}\), which is still reasonable at a parsec scale.

4.4 Important phenomena beyond ballistic approximation

Our consideration is exact and model independent when concerning photons and pairs: their interactions, propagation, breeding, etc. at a given distribution of the fluid Lorentz factor and a given magnetic field. The only assumption we make is the spectrum and density of seed high-energy photons, this is however not important as their energy content is negligible and the system ‘forgets’ their spectrum very soon.

On the other hand, our consideration is very approximate and is based on a simplified model when it concerns the fluid and the feedback of the particles on the fluid. How our simplifications affect the results and what we would obtain with a more realistic hydrodynamical treatment of the problem?

First, the pressure will redistribute the Lorentz factor of the fluid. This will hardly change significantly the process of particle breeding. More important, the formation of internal shocks at regions of maximal deceleration can increase the radiation efficiency by accelerating charged particles.

Then, we can expect that a turbulent layer near the jet boundary will be formed due to the large shear gradient of the Lorentz factor. The same can happen due to the Kelvin–Helmholtz instability of the boundary discontinuity (De Young 1986), however for an ultra-relativistic jet this instability develops slowly. The radiative deceleration of the outer layer of the jet can generate the turbulent mixing layer much earlier. Then the turbulent layer should again contribute to the radiation due to diffusive particle acceleration (see Stawarz & Ostrowski 2003).

Finally, we ignore adiabatic heating of relativistic electrons while the jet (comoving) compression ratio in \(z\) direction is \(\sim \Gamma_j^2/\Gamma\), where \(\Gamma\) is the Lorentz factor of the decelerated fluid. The account of the adiabatic heating is not simple, because the jet can expand in the transversal direction. The compression also leads to the amplification of the magnetic field \(B_j \propto 1/\Gamma\) (neglected in our simulations), which would in turn increase the role of synchrotron radiation in the decelerated part of the jet.

The formation of shocks, turbulence and adiabatic heating of electrons, which can be caused by the jet deceleration, should increase the radiative efficiency of photon breeding mechanism, while the magnetic field amplification probably decreases it. These phenomena are interesting and should be studied in future simulations.

4.5 Origin of the seed high-energy photons

In the presented simulations the energy content of the seed high-energy photons, which initiate the further evolution of the system, was taken to be five to seven orders of magnitude smaller that the final steady-state total energy content in photons within the jet. Where these initial photons can originate from? They can be associated with the shock acceleration of charged particles in the jet. There is, however, a minimum possible source of high-energy, seed photons provided by the extragalactic gamma-ray background. The observed gamma-ray background intensity at Earth at \(\epsilon > 10^3\) GeV \(cm^{-2} s^{-1} sr^{-1}\) (Sreekumar et al. 1998), corresponding to the energy density \(6 \times 10^{-19}\) erg \(cm^{-3}\). This would give the energy \(\sim 3 \times 10^{17} R_{1.6}^3\) erg within the considered cylindrical volume of radius \(R_j\) and height \(2R_j\).

We thus made a simulation (run 30) where the total energy of the seed high-energy photons in the simulation volume was 20 orders of magnitude smaller (approximately corresponding to the energy of the extragalactic gamma-ray background) than the jet energy in the same volume \(E_j = 10^{43}\) erg. The result is shown in Fig. 12. The system passes 20 orders of magnitude in the total photon energy during \(3000R/c \sim 3\) yr. A jump at the very beginning of simulations corresponds to almost immediate conversion of seed photons into pairs with the corresponding energy increase by a factor
\[ \Gamma_j^2 = 400. \] The photon energy grows exponentially with the time constant \( t_{gb} = 2.7 \) at \( t \lesssim 25 \) and \( t_{gb} = 8.2 \) at later time. The rapid rise at \( t < 20 \) corresponds to the growth of the photon avalanche as it moves downstream with the flow. At later times the growth is supported by the spatial feedback loop due to upstreaming photons. The final steady-state regime does not depend on the initial density of high-energy photons. This numerical experiment means that a jet, with parameters corresponding to run 30, would radiate half of its total energy in three years just due to the photon breeding starting off the extragalactic gamma-ray background.

5 Astrophysical Implications

5.1 Spectral energy distribution of blazars

Blazars demonstrate two-component spectra. The low-energy component peaking in the IR–X-ray range (the flares in the TeV blazars show hard X-ray spectra peaking above 100 keV) is traditionally interpreted as synchrotron radiation from relativistic electrons. The high-energy component is the Comptonized radiation from some seed soft photons. The spectra of low-luminosity objects (TeV blazars, BL Lacs) are well described by the SSC models. In high-luminosity blazars, both synchrotron and Compton components peak at lower energies (so-called blazar sequence, Fossati et al. 1998; but see Giommi et al. 2007). The role of the external radiation (from BLR or dusty torus) in providing seed photons is probably more important, and the spectra can be described by ERC model (Sikora, Begelman & Rees 1994; Sikora et al. 1997). In all objects, the two components are rather well separated.

The spectra, predicted by the photon breeding model (see Fig. 6a), demonstrate similar features. At low luminosities and compactness (runs 04, 14–15), the mean Lorentz factor of the electron–positron distribution is large (see Fig. 9). In spite of the fact that (in the jet frame) the magnetic energy density is one to two orders of magnitude smaller than that of the isotropic radiation (i.e. \( \ell_b \ll \ell_{iso}\Gamma_j^2 \), see Table 1), the synchrotron power strongly dominates over the external Compton, because the external photons interact with the high-energy pairs in the Klein–Nishina regime. As most of the synchrotron photons are also above the Klein–Nishina cut-off \( \sim 1/\gamma \), the SSC is weaker than the synchrotron.

At higher luminosities (and compactness), the high-energy photons produce a pair cascade. This reduces the mean energy per pair (see Fig. 9, runs 01–03, 10–13). At these compactness the pairs also cool more efficiently producing a cooling distribution \( dN/d\gamma \propto \gamma^{-2} \) (see Section 3.7), which changes to a steeper \( \gamma^{-3} \) behaviour at higher energies as a result of pair cascade. The latter part of the pair energy distribution is responsible for the flat part of photon spectrum (in \( E^2 dN/dE \) units). The reduction of the mean pair energy results in a shift of the photon spectra to lower energies (Fig. 6a). It also leads to the increased role of the ERC, because now most of external photons interact with pairs in Thomson regime.

The properties of our model are the increasing role of the ERC over SSC and synchrotron with luminosity and a shift of the spectral peaks to lower energies. These are in general agreement with the observational trends. However, there are some discrepancies between the shapes of the theoretical and the observed spectral shapes. At low luminosities, the synchrotron peak in our model is in the 100 MeV–1 GeV range, while it is normally observed in the X-ray range. One need to note here that the angle-dependent spectra at \( \theta \gtrsim 1/\Gamma_j \) have sharper features (see Fig. 7) and the synchrotron spectrum peaks at slightly lower energies that the spectrum averaged over \( 10^2 \) around the jet axis. Another possible reason for the discrepancy is that the electron distribution is broad and extends to very high energies. This is a consequence of our assumed spectrum of the soft isotropic radiation extending to a very low-energy \( \gamma_{min} = 10^{-9} \). A narrower and harder distribution of external soft photons might make the injection function of pairs narrower and softer, so that the maximum pair energy is below \( \gamma_{max} \) given by equation (13), reducing thus the energy of the synchrotron cut-off.

At high luminosities, our model predict basically a single component where the synchrotron and ERC components are mixed, while there are clearly two separated components in the data. However, there is no consensus whether the two components are cospatial. For example, the bright blazar 3C 279 did not show almost any variability in the radio–optical band, when the gamma-ray flux changed by an order of magnitude (Wehrle et al. 1998). Thus the radio-to-optical emission in the high-luminosity sources can be produced in a separate region, far away from the black hole.

In our model, the pairs escaping from the region filled with soft photons still carry a considerable (a few per cent) fraction of the jet energy (see Fig. 10). If these pair are reheated at larger scales (e.g. by a diffusive acceleration by various plasma perturbations), where soft radiation field is weaker, they will radiate most of their energy in the form of synchrotron. At the expense of 3–5 per cent of the jet energy for pair reheating, the synchrotron peak observed in low-peak blazars could be reproduced. If this hypothesis is valid then the high- and the low-energy peaks have different origin: the high-energy peak is a mixture of prompt synchrotron and Compton radiation of high-energy pairs in the fast cooling regime. The low-energy peak is the synchrotron radiation of pairs in a heating/cooling balance. In such a scenario the intensity of high- and low-energy peaks should correlate in time, but in a loose manner, the correlation should be stronger at longer time-scales.3

---

3 One should note here that the pair cascade does not degrade the pair energies infinitely, when the energy of the photon in the jet frame drops below \( 1/\gamma_{max}\Gamma_j \sim 10^4 \), it can easily escape and the cascade stops.
5.2 Electron energy distribution in BL Lac objects and particle acceleration

One of the most often used scenarios in the recent years for formation of the relativistic electrons, responsible for the observed emission, involves the diffusive (Fermi) acceleration at relativistic collisionless shocks (or shear layers). It has been claimed that the acceleration at relativistic shocks produces the power-law particle spectrum \( dN/dy \propto y^{-p} \) with a universal \( p = 2.2 \) index (see e.g. Achterberg et al. 2001; Keshet & Waxman 2005) which is close to the value observed in BL Lacs (Ghisellini, Celotti & Costamante 2002). These results, however, were based on certain simplifying assumptions regarding the scattering of particles by magnetic inhomogeneities. Using accurate Monte Carlo simulations with a more realistic magnetic field structure, Niemiec & Ostrowski (2006) demonstrated that no universal power law is produced and questioned the role of the Fermi-type particle acceleration mechanism in relativistic shocks.

Using particle-in-cell simulations, Spitkovsky (2007) recently showed that the electrons can be heated by interaction with ion current filaments in the upstream region reaching almost an energy equipartition with protons. The low-energy cut-off appears at \( \gamma_{\text{min}} \sim (1/5)\Gamma j_{\text{d}} m_e/c^2 \). In internal shock model, the relative velocity of colliding shells is mildly relativistic and thus we expect \( \gamma_{\text{min}} \sim 500 \). At this stage, it is too early to say whether the model would be able to produce a power-law electron distribution extending to very high energies.

The detailed fitting of the broad-band spectra of TeV blazars and low-power BL Lacs with the SSC model shows that the distribution of relativistic electrons injected to the system can be modelled as a power law of index \( p \approx 2.2 \) with the low-energy cut-off at \( \gamma_{\text{min}} \sim 10^{-6} - 10^{5} \) and the high-energy cut-off at \( \gamma_{\text{max}} \sim 10^{6} - 10^{8} \) (Ghisellini, Celotti & Costamante 2002; Krawczynski, Coppi & Aharonian 2002). Such a peaked distribution of injected electrons is not consistent with a diffusive process.

The photon breeding mechanism, on the other hand, predicts the injection spectrum to be bounded and to mirror (relative to \( m_e c^2 \)) the spectrum of the soft photon background, because the pairs in the jet are produced only by those high-energy photons that can interact with the soft photons. For example, if soft photons are from the accretion disc of maximum temperature \( \theta_{\text{max}} \), the low-energy injection cut-off is at \( \gamma_{\text{min}} \sim \Gamma \theta_{\text{max}} \) (see SP06; factor \( \Gamma \) comes from the Lorentz transformation to the jet frame). This cut-off should depend weakly on the luminosity and the black hole mass, which defines the characteristic emission radius, so that \( \theta_{\text{max}} \approx 10^{-2} L_{\Delta 45}^{1/4} (M_{\rm BH}/10^8 M_\odot)^{-1/2} \) and thus we can predict that

\[
\gamma_{\text{min}} \approx 3 \times 10^5 \left( \frac{\Gamma \theta_{\text{max}}}{20} \right) \left( \frac{L_{\Delta 45}}{10^{45} \text{ erg s}^{-1}} \right)^{-1/4} \left( \frac{M_{\rm BH}}{10^8 M_\odot} \right)^{1/2}.
\]

At high compactness, however, the synchrotron photons from the jet can provide enough opacity (see Section 4.1) and \( \gamma_{\text{min}} \) may be smaller.

For the conditions appropriate for AGN, the high-energy cut-off of the pair distribution \( \gamma_{\text{max}} \), that can participate in photon breeding, is defined by the different physics. An electron (or positron) of Lorentz factor higher than that given by equation (13) loses most of its energy to the synchrotron emission which escapes freely from the jet. Thus, at low compactness the pairs are injected to the jet between \( \gamma_{\text{min}} \) and \( \gamma_{\text{max}} \). At high compactness, because of the higher opacity the Compton scattered photons cannot easily escape from the jet, producing a pair cascade which degrades their energy (see Fig. 9). The range of Lorentz factors of injected pairs as predicted by the photon breeding mechanism is in general agreement with observations of BL Lacs.

5.3 Jet power and composition

In many models of the high-energy emission from relativistic jets, the radiative efficiency is low because only internal energy of the jet can be dissipated (e.g. in internal shock model) and only a small fraction of the energy is transferred to the (high-energy) electrons. This leads to the large jet power requirements.

The photon breeding mechanism has important properties that significantly reduce the energy budget required: (i) it produces only electrons (positrons) of high Lorentz factors; (ii) it efficiently deaccelerates the jet, using thus most of its total power. Thus the radiative efficiency is extremely high, reaching in many cases 50–80 per cent.

The primary composition of the jet is not constrained if the photon breeding works, except the general requirement that it should not be dominated by cool pairs. Indeed, a dynamically important component of cold pairs can be excluded because of the absence of the bulk Compton scattering bump produced by such pairs in the soft X-rays (Sikora & Madejski 2000). Moreover, large contribution of pairs to the bulk energy might be problematic, because of their short annihilation time in the vicinity of the black hole (Blandford & Levinson 1995). Magnetically dominated jet is less favourable for photon breeding at \( \Gamma < 20 \), while for a larger Lorentz factor the radiative efficiency is not sensitive to the jet magnetization.

Independently of the primary jet composition the photon breeding loads the jet with a significant amount of relativistic pairs. The contribution of these pairs to the jet energy flux according to our simulations is 2–5 per cent (see Section 3.7). This is probably an underestimate as we do not take into account diffusive acceleration and adiabatic heating of pairs. The number ratio of generated electrons and positrons to protons (in the case of matter-dominated jet) may be related to the mean electron random Lorentz factor (as measured in the jet frame) and the radiative efficiency:

\[
\frac{\tau_e}{\tau_0} \approx \frac{m_e \epsilon_{\text{eff}}}{m_\gamma } \langle \gamma \rangle,
\]

For low-power jets, a typical \( \gamma \sim 10^5 - 10^6 \), and the number of generated pairs should be relatively small. At high powers, the mean pair energy decreases and the generated pairs dominate (Section 3.7). Thus, for high-power quasars the model predicts the number of pairs exceeding in number the protons, while dynamically the protons still dominate. This is consistent with the constraints on the pair content obtained from the X-ray spectra of blazars associated with quasars (Sikora & Madejski 2000).

5.4 Conditions for photon breeding and gamma-ray emission sites

The arguments based on the gamma-ray transparency and the observed short time-scale variability constrain the gamma-ray emitting region in blazars to distances about \( \sim 10^{17} \) cm (Sikora et al. 1994). This distance is often associated with the BLR. In the internal shocks models, the shells of Lorentz factors \( \Gamma_1 \) and \( \Gamma_2 \) ejected from the central source and initially separated by the distance \( R_0 \)

\[
\text{(36)}
\]

\[\text{For low-power jets, a typical } \gamma \sim 10^5 - 10^6, \text{ and the number of generated pairs should be relatively small. At high powers, the mean pair energy decreases and the generated pairs dominate (Section 3.7). Thus, for high-power quasars the model predicts the number of pairs exceeding in number the protons, while dynamically the protons still dominate. This is consistent with the constraints on the pair content obtained from the X-ray spectra of blazars associated with quasars (Sikora & Madejski 2000).}
collide at the distance $R = R_0 \Gamma_1^2 / [1 - (\Gamma_1 / \Gamma_2)^2]$. Taking $R_0 = 10^{20}$ cm ($\approx 30 R_S$ for a $10^9 M_\odot$ black hole), $\Gamma_1 = 10$ and $\Gamma_2 \gg \Gamma_1$ we get $R = 10^{17}$ cm. However, the agreement with the aforementioned constraints is rather coincidental, because the black hole mass can vary by three to four orders of magnitude and there is no physical theory yet predicting the assumed separation between the shells.

The photon breeding mechanism allows various emission sites. If the jet is already accelerated and collimated at distances $\sim 100 R_S$ from the black hole, the direct radiation from the accretion disc can serve as a target for high-energy photons for pair production and to trigger the photon avalanche. The photon–photon opacity through the jet is very large at these distances and the jet deceleration and radiative efficiency might be rather small, because only a very thin boundary layer is active. The escaping radiation should have a high-energy cut-off at tens of GeV rather than at TeV energies. At larger distances the disc radiation becomes more beamed along the jet and the disc photons do not interact anymore with the high-energy radiation produced in the jet. Thus the photon breeding stops. The jet now is, however, loaded with high-energy photons that can serve as seed high-energy radiation for the avalanche to be triggered at larger distances, where the conditions for photon breeding are satisfied. The natural scale for that is the position of the BLR, where the density of the isotropic soft photons is sufficiently high. As we showed in Section 3, the radiative efficiency here can be very large.

At even larger distances, the BLR density drops, the jet becomes transparent for high-energy photons and the photon breeding stops. If at the parsec scale, the jet is still relativistic enough, the process can start operating again on the IR radiation from the dusty torus. The typical dust temperature is $T_{\text{dust}} = kT_{\text{dust}}/m_c c^2 \approx 10^7 L_{45}^{1/4} R_{pc}^{-3/2}$. The pair production optical depth is about

$$\tau_{\gamma \gamma} = \frac{n_{\text{ph,dust}}(0.2 \sigma_T) R_j}{30 \eta_j (20 \theta) L_{45}^{1/2} R_{pc}^{-3/2}},$$

where $n_{\text{ph,dust}} = 0.37 T_{\text{dust}}/kT_{\text{dust}}$ is the number density of photons from the dust and $\eta_j$ is the ratio of the dust to the disc luminosities. Thus, even for $\eta_j$ of the order of a few per cent, the photon breeding is effective at the parsec scale in bright quasars.

It has not escaped our attention that the jet may become active even further out: by interacting at kpc scale with the stellar radiation field and at $\sim 100$ kpc with the cosmic microwave background radiation.

We note here that photon breeding works well at high disc luminosities (see Section 3.3) characteristic for quasars. In BL Lac objects, where the discs are less luminous, photon breeding may operate at small distance scale, which in turn requires small black hole mass and/or fast jet acceleration, or for large jet Lorentz factor $\Gamma_1 \gtrsim 40$. The observed fast variability from PKS 2155–304 (Aharonian et al. 2007) and Mrk 501 (Albert et al. 2007) supports these suggestions.

### 5.5 The Doppler factor crisis in TeV blazars

The Doppler factors required by the homogeneous SSC models to describe the spectra of the blazars emitting at TeV energies (to avoid absorption by the IR radiation), is rather large $\delta \sim 50$–200 (Ghisellini et al. 2002; Krawczynski et al. 2002; Konopelko et al. 2003; Giebels et al. 2007). Such high $\delta$ values disagree with the small apparent velocities observed at the parsec scale in Mrk 421 and Mrk 501 (Marscher 1999; Piner & Edwards 2005) and other TeV blazars (Piner & Edwards 2004).

One proposed solution to this $\delta$-crisis (Tavecchio 2005) is that the jet Lorentz factor drops from 15 at the gamma-ray emitting, subparsec scale to $\sim 4$ at the radio-emitting very long baseline interferometry (VLBI) parsec scale (Georganopoulos & Kazanas 2003). For the viewing angle within the beaming pattern of the initial jet, $\theta \lesssim 1/\Gamma_j$, the apparent velocity of the decelerated jet with Lorentz factor $\Gamma_\text{f} \ll \Gamma_j$ is

$$\beta_{\text{f,app}} = \frac{\beta_j \sin \theta}{1 - \beta_j \cos \theta} \approx \frac{2 \theta \Gamma_j^2}{1 + (\theta \Gamma_j)^2} \approx 2 \theta \Gamma_j^2 \lesssim 2 \Gamma_j^2.$$  

Thus, deceleration of the jet to $\Gamma_\text{f} < \sqrt{\Gamma_j^2 / 2}$ guaranties that the apparent motion is subluminal.

The question arises what is the mechanism that decelerates the jet at subparsec scale. The internal shocks in the jet (Spada et al. 2001) are rather inefficient unless huge fluctuations of the Lorentz factors are involved (Beloborodov 2000), which seems unlikely. On the other hand, the photon breeding mechanism predicts significant deceleration of the jet (see Table 1) and strong emission at subparsec scale, if the conditions for photon breeding are satisfied. The photon breeding thus may be responsible for jet deceleration and resolution of the $\delta$-crisis.

A different way to solve the $\delta$-crisis is to assume that the jet consists of a fast spine and a slow sheath (Chaberge et al. 2000; Ghisellini, Tavecchio & Chiaberge 2005). In this model a slower sheath having a softer spectrum dominates the emission in the radio band. The photon breeding mechanism produces exactly such a structure (Fig. 4) and the spectra (Fig. 8) in a self-consistent way.

Thus, the jet behaviour predicted by the photon breeding mechanism unites the two proposals: it decelerates the jet at subparsec scales and produces a fast spine–slow sheath structure.

### 5.6 Emission pattern

#### 5.6.1 Unification of BL Lacs and FR I radio galaxies

According to the unification scheme of radio-loud active galaxies (Urry & Padovani 1995), BL Lac objects are Fanaroff–Riley type I (FR I) radio galaxies with their jets oriented close to the line of sight. The average Lorentz factor of the jets, derived by matching the luminosity functions and statistics of BL Lac and FR I (and B2) samples, was estimated to be $\Gamma_j \sim 3–5$ (Urry & Padovani 1995; Hardcastle et al. 2003). The core optical luminosities of BL Lacs are on average $10^{43}$ times higher than those of FR I (Chiaberge et al. 2000) with the same extended radio luminosity. Associating the core emission with the jet, we again get rather low Lorentz factors $\Gamma_1 \approx 6$ or 4 for the continuous steady jet or a moving blob, respectively. These low $\Gamma_1$ are in clear disagreement with the much higher values of the Doppler factors required to explain the gamma-ray emission of BL Lacs.

Both decelerating (Georganopoulos & Kazanas 2003) and structured (Chiaberge et al. 2000; Ghisellini et al. 2005) jet models provide explanations for the discrepancy. Because the photon breeding mechanism produces decelerating and structured jet, it obviously is also capable of unifying BL Lacs with the radio galaxies, keeping high $\Gamma_1$ to explain the gamma-ray emission. In blazars the emission from the fast, $\Gamma_1 \approx 20$, spine dominates. In radio galaxies observed at large angles $\theta \sim 1$ (see Fig. 8), the optical emission is produced in the slower sheath of $\Gamma = 2–6$. 

5.6.2 Off-axis emission and the TeV emission from radio galaxies

As we have discussed above, the photon breeding mechanism naturally produces very broad beams of photons (see also Derishev et al. 2003; Derishev, Aharonian & Kocharyan 2007). The gamma-ray emission at $\theta \sim 1$ is produced in the external environment (see Fig. 8). The luminosity ratio between the nearly isotropic emission and the beam emission at $\theta \approx 1/\Gamma_j$ is about $\Gamma_j^{-4}$ (two powers of $\Gamma_j$ come from the energy amplification in the jet and two powers appear because of beaming). This ratio is $\sim \Gamma_j^{-7}/10$ larger than that predicted by equation (20). Thanks to the emission from the external medium, the nearby misaligned jets become observable in high-energy gamma-rays.

The central source of M87, which has the best studied jet, has a rather low disc luminosity of only $\sim 10^{36}$ erg s$^{-1}$ (Biretta, Stern & Harris 1991). With the threshold $L_\delta > 10^{33} R_{17}^2$ erg s$^{-1}$ for $\Gamma_j = 20$ the photon breeding in model A is possible at $R < 10^{16}$ cm, which is only $\sim 10 R_\delta$ for the estimated mass of the central black hole $\sim 3 \times 10^6 M_\odot$ (Macchetto et al. 1997). At such a distance the photon breeding will operate on the direct disc radiation (model C). The implied distance is consistent with the detection of the rapid ($\sim 10^7$ s) variability of the TeV photon flux from M87 (Aharonian et al. 2006). However, photon breeding may not operate, if the wide pattern at the base of the jet observed by VLBI (Junor, Biretta & Livio 1999, but see Krichbaum et al. 2007) actually reflects the jet geometry, which would mean that the opening angle is large.

5.7 Observational appearance and volume dissipation

Most of the emission from the jet undergoing photon breeding comes from the regions of maximum gradient of $\Gamma_j$. In the steady state, the volume emissivity contributing to the observed emission (at small angles to the jet) is

$$ j(r, z) \propto \frac{d\Gamma_j(r, z)}{dz} \delta^3 \Gamma_j. $$

(39)

In the case of small luminosities (and small $\Gamma_j$) only the outer layers of the jet suffer significant deceleration (see Fig. 4b, run 24), resulting in limb-brightening, with most of the emission coming from large $z$, where the cascade had time to develop. The situation is more complicated at high luminosities (or large $\Gamma_j$). The outer layers decelerate rapidly (see curves for runs 21–23 in Fig. 5) making the emission limb-brightened at small $z$, while the layers close to the jet axis decelerate slower. Thus the emission from the core dominates at large $z$. At angles larger than $\gtrsim 1/\Gamma_j$, only slower, significantly decelerated layers contribute to the observed luminosity, and therefore we always would see the limb-brightened emission.

Our predictions are consistent with the observed limb-brightened morphology of the Mrk 501 jet at the parsec scale (Giroletti et al. 2004). Such a structure could result from the efficient deceleration and loading by relativistic pairs of the jet outer layers by the photon breeding at a subparsec scale.

6 CONCLUSIONS

The photon breeding mechanism can be an extremely efficient way of dissipating bulk energy of relativistic ($\Gamma_j \gtrsim 10$) jet into high-energy radiation. In the case of high luminosity AGN and powerful jets, the mechanism is very robust: it works at any value of the jet magnetic field and is not sensitive to the spectrum of the external radiation. At high luminosities and jet Lorentz factors, the mechanism should work almost equivalently, the only fact that can prevent the runaway photon breeding is a purely longitudinal (along the jet) geometry of the magnetic field.

At the intermediate range of AGN luminosity, $10^{43} < L_{43} R_{17} < 3 \times 10^{44}$ erg s$^{-1}$ and the Lorentz factor above 10, the mechanism still can work efficiently, but only at favourable conditions: a soft spectrum of external isotropic radiation and a weak (dynamically not important) magnetic field. When the Lorentz factor is below $\sim 8$ or the AGN luminosity is below $10^{43} R_{17}$ erg s$^{-1}$ the photon breeding mechanism does not work.

The mechanism can work in different astrophysical contexts: in the immediate vicinity of the accretion disc, in the broad line region (probably, most efficiently), and in the IR radiation field produced by the dust at a parsec scale. There could be other sites for operation of the photon breeding mechanism (e.g. stellar radiation field at a kpc scale, cosmic microwave background radiation at 100-kpc scale).

There exists a clear signature of the mechanism which can be observed by GLAST in the spectra of moderately bright blazars: a synchrotron cut-off at a few GeV range.

There exists some problem with the straightforward interpretation of the blazar spectra. The low-energy synchrotron peak reproduced by our simulations is less prominent than the one observed in the spectra of gamma-ray quasars. An additional mechanism of gradual pair reheating is necessary. This could be associated with a diffusive Fermi acceleration of pairs, produced by the photon breeding, by fluid perturbations. Such reheating mechanism should have a moderate energy budget and seems very natural after a strong impact of radiation on the jet. Importantly, the photon breeding solves the problem of injection of relativistic electrons for Fermi acceleration: they are already produced by high-energy photons.

Fast deceleration of the outer jet layers results in the fast spine-slower sheath structure which is also implied by various observations. Particularly, the differential deceleration can resolve the contradiction between a requirement of the large Doppler factor in the gamma-ray emitting region and the low Lorentz factor of jets in BL Lacs derived from the radio and optical observations.

Despite the fact that the photon breeding mechanism has not been known before and may seem somewhat exotic, it is actually much simpler in the description than the diffusive Fermi acceleration, which depends on complicated plasma phenomena. Once the velocity pattern for the fluid, the magnetic field and the external radiation field are specified, the fate of each high-energy photon and its descendants can be reproduced (in statistical sense) from first principles, because the interaction cross-sections are known with high accuracy. The question whether a photon produces a runaway avalanche or not, can be answered exactly. However, there still remain some details which require a more elaborated treatment of the fluid dynamics and a more complete model for the jet. Particularly, it would be important to study the jet launch, the photon breeding and the jet deceleration with the resulting gamma-ray emission in one numerical experiment.

ACKNOWLEDGMENTS

The work is supported by the Russian Foundation for Basic Research grant 07-02-00629-a, the Magnus Ehrnrooth Foundation, the Vilho, Yrjö and Kalle Väisälä Foundation, and the Academy of Finland grants 110792 and 112982. We thank Anatoly Spitkovsky and Amir Levinson, the referee, for comments.

REFERENCES

Aharonian F. et al., 2006, Sci, 314, 1424