## Tilings and Patterns: Homework 5 (13.10.2025)

- 1. A domino is  $2 \times 1$  rectangle. For each of the seven frieze groups, find a monohedral tiling of the plane by dominoes that has this group as the symmetry group.
- 2. Prove that every hexagon with three pairs of equally long parallel sides is a prototile of a monohedral tiling.
- 3. Prove that every triangle and every quadrilateral (that is, 4-gon) is a prototile of a monohedral tiling.
- 4. Prove that the symmetry group of an *n*-isohedral tiling is a wallpaper group.
- 5. Converse to the previous problem: show that a k-hedral tiling whose symmetry group is a wallpaper group is n-isohedral, for some n.
- 6. Determine the symmetry groups of the 11 archimedean tilings.
- 7. Determine the transitivity classes of the 11 archimedean tilings.